

Subadditivity inequalities in von Neumann algebras and characterization of tracial functionals

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Abstract

We examine under which assumptions on a positive normal functional φ on a von Neumann algebra, M and a Borel measurable function $f: \mathbb{R}^+ \rightarrow \mathbb{R}$ with $f(0) = 0$ the subadditivity inequality $\varphi(f(A+B)) \leq \varphi(f(A)) + \varphi(f(B))$ holds true for all positive operators A, B in M . A corresponding characterization of tracial functionals among positive normal functionals on a von Neumann algebra is presented. © Springer 2005.

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Keywords

Algebra of matrices, Functional calculus, Positive normal functional, Subadditivity inequality, Tracial functional, Von Neumann algebra